

Convection heat transfer is expressed by Newton’s law of cooling as

$$q_{conv} = h \cdot A_s \cdot (T_s - T_\infty)$$

Where

- $h$  is the convection heat transfer coefficient,
- $T_s$  is the surface temperature, and
- $T_\infty$  is the free-stream temperature.

The convection coefficient is also expressed as

$$h = \frac{-k_{fluid} \cdot \left(\frac{\partial T}{\partial y}\right)_{y=0}}{(T_s - T_\infty)}$$

The dimensionless heat transfer coefficient, called the **Nusselt number (Nu)**, is defined as

$$Nu = \frac{h \cdot L_c}{k}$$

Where

- $k$  is the thermal conductivity of the fluid,
- $L_c$  is the characteristic length.

The friction force per unit area is called **shear stress**( $\tau_s$ ), and the **shear stress** at the wall surface is expressed as

$$\tau_s = \mu \cdot \left.\frac{\partial u}{\partial y}\right|_{y=0} \quad \text{or} \quad \tau_s = C_f \cdot \frac{\rho \cdot V^2}{2}$$

Where

- $\mu$  is the dynamic viscosity,
- $V$  is the upstream velocity, and
- $C_f$  is the dimensionless friction coefficient.

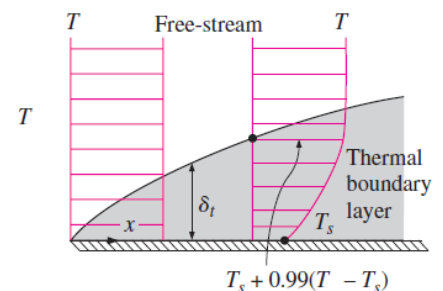
The property ( $\nu = \mu/\rho$ ) is the kinematic viscosity.

The friction force over the entire surface is determined from

$$F_f = C_f \cdot A_s \cdot \frac{\rho \cdot V^2}{2}$$

The flow region over the surface in which the temperature variation in the direction normal to the surface is significant is the **thermal boundary layer**( $\delta_t$ ).

The thickness of the thermal boundary layer  $\delta_t$  at any location along the surface is the distance from the surface at which the temperature difference  $T - T_s$  equals  $0.99(T_\infty - T_s)$ .



## SUMMARY – EXTERNAL FORCED CONVECTION HEAT TRANSFER

The relative thickness of the velocity and the thermal boundary layers, ( $\delta$ ) and ( $\delta_t$ ) respectively, is best described by the dimensionless **Prandtl number (Pr)**, defined as

$$Pr = \frac{v}{\alpha} = \frac{\mu \cdot C_p}{k}$$

For external flow, the dimensionless **Reynolds number (Re)** is expressed as

$$Re = \frac{V \cdot L_c}{\nu} = \frac{\rho \cdot V \cdot L_c}{\mu}$$

For a flat plate, the characteristic length is the distance ( $x$ ) from the leading edge. The Reynolds number at which the flow becomes turbulent is called the **critical Reynolds number**. For flow over a flat plate, its value is taken to be

$$Re_{cr} = \frac{V \cdot x_{cr}}{\nu} = 5 \times 10^5$$

The **drag coefficient ( $C_D$ )** is a dimensionless number that represents the drag characteristics of a body, and is defined as

$$C_D = \frac{F_D}{\frac{1}{2} \cdot \rho \cdot V^2 \cdot A}$$

Where

$A$  is the frontal area for blunt bodies, and surface area for parallel flow over flat plates or thin airfoils.

For flow over a flat plate, the Reynolds number is

$$Re = \frac{V \cdot x}{\nu} = \frac{\rho \cdot V \cdot x}{\mu}$$

Transition from laminar to turbulent occurs at the *critical Reynolds number* of

$$Re_{x,cr} = \frac{V \cdot x_{cr}}{\nu} = 5 \times 10^5$$

## FOR PARALLEL FLOW OVER A FLAT PLATE

The local friction coefficient ( $C_{f,x}$ ) and convection coefficient ( $Nu_x$ ) are

Regime flow	Correlation	Condition
Laminar	$C_{f,x} = \frac{0.664}{Re_x^{1/2}}$	$Re_x < 5 \times 10^5$ $Pr > 0.6$
	$Nu_x = \frac{h_x \cdot x}{k} = 0.332 Re_x^{0.5} Pr^{1/3}$	
Turbulent	$C_{f,x} = \frac{0.059}{Re_x^{1/5}}$	$5 \times 10^5 \leq Re_x \leq 10^7$ $0.6 \leq Pr \leq 60$
	$Nu_x = \frac{h_x \cdot x}{k} = 0.0296 Re_x^{0.8} Pr^{1/3}$	



## SUMMARY – EXTERNAL FORCED CONVECTION HEAT TRANSFER

The **average friction coefficient** ( $C_f$ ) relations for flow over a flat plate are:

Regime flow	Correlation	Condition
Laminar	$C_f = \frac{1.33}{Re_L^{1/2}}$	$Re_L < 5 \times 10^5$
Turbulent	$C_f = \frac{0.074}{Re_L^{1/5}}$	$5 \times 10^5 \leq Re_L \leq 10^7$
Combined	$C_f = \frac{0.074}{Re_L^{1/5}} - \frac{1742}{Re_L}$	$5 \times 10^5 \leq Re_L \leq 10^7$

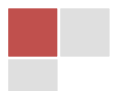
The **average Nusselt number** ( $Nu$ ) relations for flow over a flat plate are:

Regime flow	Correlation	Condition
Laminar	$Nu = \frac{h.L}{k} = 0.664Re_L^{0.5}Pr^{1/3}$	$Re_L < 5 \times 10^5$
Turbulent	$Nu = \frac{h.L}{k} = 0.037Re_L^{0.8}Pr^{1/3}$	$5 \times 10^5 \leq Re_L \leq 10^7$ $0.6 \leq Pr \leq 60$
Combined	$Nu = \frac{h.L}{k} = (0.037Re_L^{0.8} - 871)Pr^{1/3}$	$5 \times 10^5 \leq Re_L \leq 10^7$ $0.6 \leq Pr \leq 60$

### FOR ISOTHERMAL SURFACES WITH AN UNHEATED STARTING SECTION OF LENGTH ( $\xi$ )

Regime flow	Correlations for local Nusselt Number ( $Nu_x$ )
Laminar	$Nu_x = \frac{Nu_x(\text{for } \xi=0)}{\left[1 - (\xi/x)^{3/4}\right]^{1/3}} = \frac{0.332Re_x^{0.5}Pr^{1/3}}{\left[1 - (\xi/x)^{3/4}\right]^{1/3}}$
Turbulent	$Nu_x = \frac{Nu_x(\text{for } \xi=0)}{\left[1 - (\xi/x)^{9/10}\right]^{1/9}} = \frac{0.0296Re_x^{0.8}Pr^{1/3}}{\left[1 - (\xi/x)^{9/10}\right]^{1/9}}$

Regime flow	Correlations for the average convection coefficient ( $h$ )
Laminar	$h = \frac{2 \left[1 - (\xi/x)^{3/4}\right]}{1 - \xi/L} h_{x=L}$
Turbulent	$h = \frac{5 \left[1 - (\xi/x)^{9/10}\right]}{1 - \xi/L} h_{x=L}$



**FOR A UNIFORM HEAT FLUX OVER A FLAT PLATE**

Regime flow	Correlations for local Nusselt Number ( $Nu_x$ )
Laminar	$Nu_x = 0.453Re_x^{0.5}Pr^{\frac{1}{3}}$
Turbulent	$Nu_x = 0.0308Re_x^{0.8}Pr^{\frac{1}{3}}$

**FOR CROSS FLOW OVER A CYLINDER AND SPHERE ARE**

Regime flow	Correlations for the average Nusselt Number ( $Nu$ )
Laminar Valid for : $Re.Pr > 0.2$	$Nu_{cyl} = \frac{h.D}{k} = 0.3 + \frac{0.62Re_x^{0.5}Pr^{\frac{1}{3}}}{\left[1 + (0.4/Pr)^{2/3}\right]^{1/4}} \left[1 + \left(\frac{Re}{282\,000}\right)^{5/8}\right]^{4/5}$
Turbulent Valid for : $3.5 \leq Re \leq 80\,000$ $0.7 \leq Pr \leq 380$	$Nu_{sph} = \frac{h.D}{k} = 2 + \left[0.4Re^{1/2} + 0.06Re^{2/3}\right] Pr^{0.4} \left(\frac{\mu_\infty}{\mu_s}\right)^{1/4}$

The fluid properties are evaluated at the film temperature  $T_f = \frac{(T_\infty + T_s)}{2}$  in the case of a cylinder, and at the freestream temperature ( $T_\infty$ ).

Except for  $\mu_s$ , which is evaluated at the surface temperature ( $T_s$ ). in the case of a sphere.

