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Homework n°01

Exercise

The bottom of a pan is made of a **4-mm-thick aluminium layer**. In order to increase the rate of heat transfer through the bottom of the pan, someone proposes a design for the bottom that consists of a **3-mm-thick copper layer sandwiched between two 2-mm-thick aluminium layers**.

Will the new design conduct heat better? Explain.

Given:

 $k_{copper} = 398 \text{ W/m.K}$ $k_{aluminium} = 237 \text{ W/m.K}$



Calculate the Thermal Resistance of the Original Design (Aluminum Only)

The formula for thermal resistance is: R=k/L

 $R = 0.004 \ / \ 237 \approx 0.00001688 \ \text{K/W}$

So, the thermal resistance of the original design is: $R_{\text{original}} = 0.00001688 \text{ K/W}$

Calculate the Thermal Resistance of the New Design (Aluminum/Copper/Aluminum)

The total thermal resistance is the sum of the resistances of each layer:

 $R_{\mathrm{new}} = R_{\mathrm{aluminum, \, top}} + R_{\mathrm{copper}} + R_{\mathrm{aluminum, \, bottom}}$

 $R_{\rm aluminum,\ total} = 2 \times 0.00000844 \approx 0.00001688\,\mathrm{K/W}$

 $R_{
m copper} = rac{L}{k} = rac{0.003}{398} pprox 0.00000754\,{
m K/W}$

 $R_{
m new} = R_{
m aluminum, \ total} + R_{
m copper}$ $R_{
m new} = 0.00001688 + 0.00000754 pprox 0.00002442 \, {
m K/W}$

The new design introduces the thermal resistance of the copper layer in addition to the thermal resistance of the aluminium which has the same value for both designs. Therefore, <u>the new design will be a poorer</u> <u>conductor of heat.</u>