

Supervised Work 4: Regular Expressions

Exercise 1

Consider the alphabet $L=\{a,b\}$.

Provide the regular expressions corresponding to the following properties:

1. Words that contain no b.
2. Words that do not contain "ab"
3. Words that contain at least one "a"
4. Words of even length.
5. Consider the alphabet $X=\{0,1\}$. Provide the regular expression for binary numbers greater than or equal to 8.

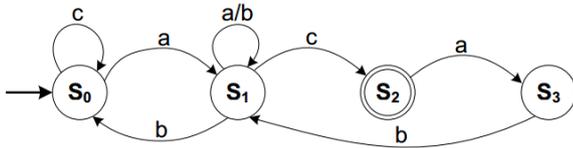
Exercise 2

Construct the deterministic finite state automata (DFA) accepting the following languages:

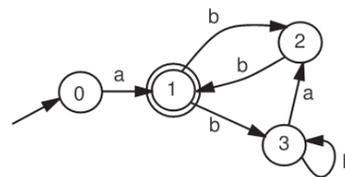
- $(A + b)^*c$
- $((a^*bc^*)^*acb^*)^*$
- $(a+b)^*ab(a+b)^*$
- $(1.1^*.0.0^*.1)^*.0.1^*$

Exercise 3

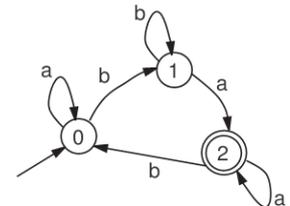
Determine the regular expression denoting the languages $L(A)$, $L(B)$, and $L(C)$ for the following automata A, B, and C:



A



B



C

Exercise 4

For each of the following regular expressions, construct a finite automaton that recognizes the same language.

1. $a^* + (bb)^*$
2. $(bba)^*(a+b)^*+b^*$
3. $(b+ab)^*(\epsilon+a)$
4. $(b^*+a)^* aa$
5. $((ab)^* ab (aa+b)^*)$

Exercise 5

Are the following languages regular? Justify your answers.

- $L1 = \{a^n b^m, n \geq 0, m > 0\}$;
- $L2 = \{a^n b^p, n \geq p\}$;
- $L3 = \{(ab)^n c^m (be)^{n+m} \text{ avec } n, m \geq 0\}$.