

## In-Class Exercises n°02

### Exercise 2.1

The temperature distribution across a wall 1 m thick at a certain instant of time is given a

$$T(x) = a + bx + cx^2$$

Where

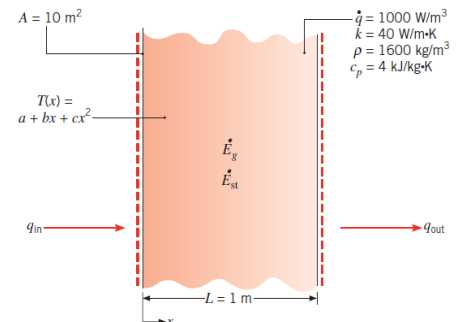
$T$  is in degrees Celsius and  $x$  is in meters

While

$a = 900^\circ\text{C}$ ,  $b = -300^\circ\text{C/m}$ , and  $c = -50^\circ\text{C/m}^2$

A uniform heat generation,  $\dot{q} = 1000 \text{ W/m}^3$ , is present in the wall of area  $10 \text{ m}^2$  having the properties

$\rho = 1600 \text{ kg/m}^3$ ,  $k = 40 \text{ W/m}\cdot\text{K}$ , and  $c_p = 4 \text{ kJ/kg}\cdot\text{K}$

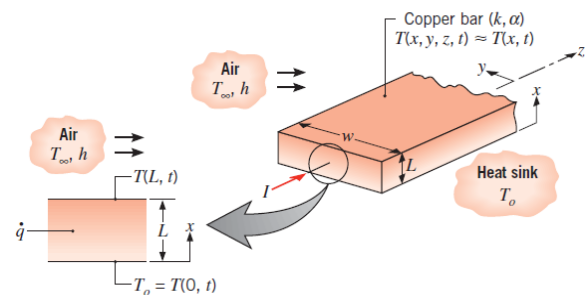


(Figure 2.1)

1. Determine the rate of heat transfer entering the wall ( $x = 0$ ) and leaving the wall ( $x = 1 \text{ m}$ ).
2. Determine the rate of change of energy storage in the wall.
3. Determine the time rate of temperature change at  $x = 0, 0.25$ , and  $0.5 \text{ m}$ .

### Exercise 2.2

A long copper bar of rectangular cross section, whose width  $w$  is much greater than its thickness  $L$ , is maintained in contact with a heat sink at its lower surface, and the temperature throughout the bar is approximately equal to that of the sink,  $T_o$ . Suddenly, an electric current is passed through the bar and an airstream of temperature  $T_\infty$  is passed over the top surface, while the bottom surface continues to be maintained at  $T_o$ .



(Figure 2.2)

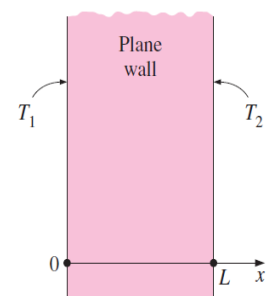
Obtain the differential equation and the boundary and initial conditions that could be solved to determine the temperature as a function of position and time in the bar.

### Exercise 2.3

Consider a large plane wall of thickness  $L = 0.2 \text{ m}$ , thermal conductivity  $k = 1.2 \text{ W/m}\cdot^\circ\text{C}$ , and surface area  $A = 15 \text{ m}^2$ . The two sides of the wall are maintained at constant temperatures of  $T_1 = 120^\circ\text{C}$  and  $T_2 = 50^\circ\text{C}$ , respectively, as shown in Figure 2-3.

Determine

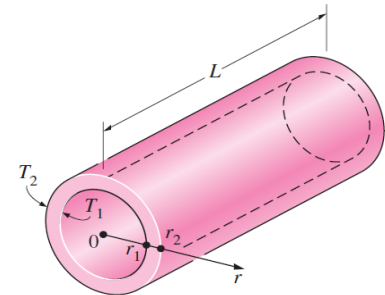
- a) the variation of temperature within the wall and the value of temperature at  $x = 0.1 \text{ m}$
- b) the rate of heat conduction through the wall under steady conditions.



(Figure 2.3)

#### Exercise 2.4

Consider a steam pipe of length  $L = 20 \text{ m}$ , inner radius  $r_1 = 6 \text{ cm}$ , outer radius  $r_2 = 8 \text{ cm}$ , and thermal conductivity  $k = 20 \text{ W/m}\cdot^\circ\text{C}$ , as shown in **Figure 2-4**. The inner and outer surfaces of the pipe are maintained at average temperatures of  $T_1 = 150^\circ\text{C}$  and  $T_2 = 60^\circ\text{C}$ , respectively.

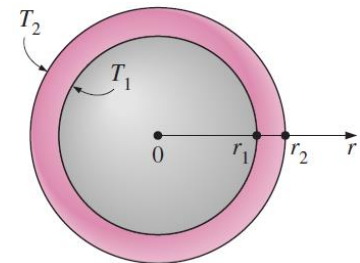


(Figure 2.4)

Obtain a general relation for the temperature distribution inside the pipe under steady conditions, and determine the rate of heat loss from the steam through the pipe.

#### Exercise 2.5

Consider a spherical container of inner radius  $r_1 = 8 \text{ cm}$ , outer radius  $r_2 = 10 \text{ cm}$ , and thermal conductivity  $k = 45 \text{ W/m}\cdot^\circ\text{C}$ , as shown in **Figure 2-5**. The inner and outer surfaces of the container are maintained at constant temperatures of  $T_1 = 200^\circ\text{C}$  and  $T_2 = 80^\circ\text{C}$ , respectively, as a result of some chemical reactions occurring inside.



(Figure 2.5)

Obtain a general relation for the temperature distribution inside the shell under steady conditions, and determine the rate of heat loss from the container.

#### Exercise 2.6

Consider, for each situation, a medium in which the heat conduction equation is given in its simplest form as

| Situation 1                                                                          | Situation 2                                                              | Situation 3                                                                                                    |
|--------------------------------------------------------------------------------------|--------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------|
| $\frac{\partial^2 T}{\partial x^2} = \frac{1}{\alpha} \frac{\partial T}{\partial t}$ | $\frac{1}{r} \frac{d}{dr} \left( rk \frac{dT}{dr} \right) + \dot{g} = 0$ | $\frac{1}{r^2} \frac{d}{dr} \left( r^2 \frac{dT}{dr} \right) = \frac{1}{\alpha} \frac{\partial T}{\partial t}$ |

- Is heat transfer steady or transient?
- Is heat transfer one-, two-, or three-dimensional?
- Is there heat generation in the medium?
- Is the thermal conductivity of the medium constant or variable?

#### Exercise 2.7

Beginning with a differential control volume in the form of a cylindrical shell, derive the heat diffusion equation for a one-dimensional, cylindrical, radial coordinate system with internal heat generation. Compare your result with Equation (Eq.02).

#### Exercise 2.8

Beginning with a differential control volume in the form of a spherical shell, derive the heat diffusion equation for a one-dimensional, spherical, radial coordinate system with internal heat generation. Compare your result with Equation (Eq.03).