

Exercises Series N°2

Exercise 1:

A uniformly charged rod of length L and total charge $+q$ lies along the y axis from $y=0$ to $y=L$ as shown in the figure.1

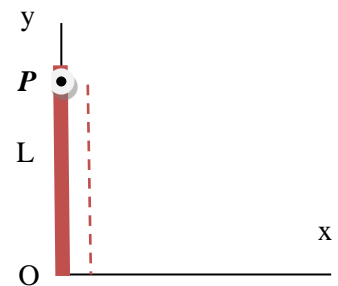


Figure.1

- a. Calculate the x - component $E_x(x)$ at the point x_0 on the x - axis.
- b. As in (a) also calculate the y - component $E_y(x)$ at the point x_0 on the x - axis. Again leave your answer in integral form.
- c. If now the charge density λ_0 of (a) becomes $\lambda(L)=\lambda_0 (y/L)$, that is increasing function of y then indicate how this would modify your answers to parts (a) and (b) as you integrate over dq .
- d. Now assume that $x_0 \gg L$, that is, $(y/x_0) \ll 1$. show that your result (b) can be written as the field from a dipole $E_y(x) = qL/8\pi\epsilon_0 x_0^3$ by approximating the sqrt-root term in the integral by using the approximation $(1+z)^n = 1+nz$, and disregarding terms in y/x_0 so that the integral becomes trivial.

Exercise 2:

A circular disk of radius a is uniformly charged with surface charge density $\sigma(C/m^2)$. If the disk lies on the $z=0$ plane (i.e., x - y plane) with its axis along the z -axis. Show that the electric field at the point $(0, 0, h)$ is given by (using two methods):

$$\vec{E} = \frac{\sigma}{2\epsilon_0} \left[1 - \frac{h}{\sqrt{h^2+a^2}} \right] \hat{a}_z$$

Exercise 3:

A sphere of radius r has electric charge uniformly distributed in its entire volume.

At a distance d from the center inside the sphere ($d < r$) the electric field intensity is directly proportional to:

- A. $1/d$
- B. $1/d^2$
- C. d
- D. d^2

Exercise 4:

There are three charges q_1 , q_2 , and q_3 having charge 6 C, 5 C and 3 C enclosed in a surface.

-Find the total flux enclosed by the surface.

Exercise 5:

A solid nonconducting sphere of radius R has a nonuniform charge distribution of volume charge density $\rho = \rho_s r/R$, where ρ_s is a constant and r is the distance from the center of the sphere. **Show** (a) that the total charge on the sphere is $Q = \pi\rho_s R^3$ and (b) that **gives** the magnitude of the electric field inside the sphere.

$$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{R^4} r^2$$