# Chapter 1(part 2): Recursion

### **1.** Notion of the recursion:

- In programming, *recursion* is a method that allows a sub-program (procedure or function) of calls herself.
- It is in <u>their part body</u> (instructions) we find a call to the procedure (or function) itself.

*Example:* write an algorithm (function) to calculate the factorial of a given integer N?

### a) Solution iterative (classic) :

N !=1\*2\* 3\*4\*5\*... \*(N-1)\*N.

**Function** fact (N: integer): integer;

R, i: integer;

# Begin

 $R \leftarrow 1$ ; For i = 1 to N do  $R \leftarrow R^* i$ :

**End For** 

Return (R);

END;

### b) Solution recursive:

N !=N\*(N-1) !

 $= N^{*}(N-1)^{*}(N-2)!$ 

 $=N^{*}(N-1)^{*}(N-2)^{*}$  .....\* 0!

➤ the function factorial "*fact*" is defined as follows :

 $\begin{array}{ll} \checkmark & \mbox{If } N=0: & \mbox{fact } (0)=1. \\ \checkmark & \mbox{If } N<>0: & \mbox{fact } (N)=N*\mbox{fact}(N-1). \end{array}$ 

> In algorithmic, the function *fact* is defined as follow :

Function fact (N: integer): integer;







### 2. Types of recursion:

- > We distinguished usually two types of recursion :
  - ✓ **simple** recursion
  - ✓ **crossed** recursion

## The simple recursion:

This is when a subroutine (function or procedure) calls itself. This is indeed the general case of recursion, as we have already seen in the previous example with the function **fact**.

### <u>Syntax :</u>

Procedure P Begin

. . .

... Call to P:

# END;

**Example** : calculation of the sum of the first **n** positive integers.

Sum (n) = 1 + 2 + 3 + ... + (n-1) + N

Function Sum (N : integer) : integer;

S: integer;

## Begin

If (n = 1) then  $S \leftarrow 1$ ;

# Else

 $S \leftarrow Sum(n-1) + n;$ 

### End if

Return (S);

END;

#### The cross recursion:

We call cross recursion the do that two procedures P1 And P2 call each other, i.e. when P1 executes, it calls P2, and when P2 executes, it calls to P1.

### Syntax:

```
Procedure P1
   Begin
       . . .
       Call to P2;
       . . .
    END:
    Procedure P2
    Begin
       Call to P1;
       . . .
   END:
Example :
\blacktriangleright A positive integer n can be either :
Even \rightarrow n = 2*k
Odd \rightarrow n = 2*k+1
> If we considered two functions Even (n) And Odd (n) has logical values
    (boolean) then we will have :
       If Even (n) = true
                               then Odd (n) = false
       If Odd (n) = true
                               then Even (n) = false
```



- 3. Rules of design :
- a) <u>First rule :</u>
- Seek to break down the problem into several below problems of the same kind but lower size.
- b) <u>Second rule :</u>
- Any recursive algorithm must distinguish several cases, at least one of which born must not include recursive call (*stop Condition Or ending*). It is the trivial case, otherwise risk of loop infinitely.

# Condition of termination:

- ✓ Non-recursive cases of a recursive algorithm are called *base cases*.
- ✓ The conditions that the data must satisfy in these base cases are called conditions of ending.

## Example :

**Function** fact (N : integer):integer ; R: integer ;

Begin Return (N \* fact (N - 1));



Call to fact(4) 4\*fact(3) = ? Apple at fact(3)

```
b) = 1:

ble at fact(3)

3*fact(2) = ?

Call to fact(2)

2*fact(1) = ?

Call has fact(1)

1*fact(0) = ?

Call to fact(0)

0*fact(-1) = ?
```

•••

Without conditions of ending?!

#### Solution :

Function fact (N: integer): Integer;

R : integer;



### Noticed :

- Since a recursive function calls itself, it is imperative that we provide for a condition stop to the recursion, otherwise the program does **never stop**.
- ➤ We must always test the stopping condition first, and then, if the condition is not verified, we start a recursive call.

# c) <u>Third rule :</u>

All call recursive must to do with data closer to the data that satisfying the termination condition.

### **Benefits of the recursion:**

- > Simplify the writing of programs, because the calculations to be performed are not explicitly defined.
- > Facilitate the task of the programmer who will no longer have to specify the number of iterations of the same action, neither have to manage the values of the different variables used.